



SEMINARIUM MATEMATYKA DYSKRETNA

wtorek, 10 marca 2026 r., godz. 12:30, s. 612 C7

3-colourability, diamonds and butterflies

Ingo Schiermeyer

WMS AGH, TU Bergakademie Freiberg

(co-authors: Nadzieja Hodur, Monika Pilśniak, Magdalena Prorok)

The 3-colourability problem is an NP-complete problem which remains NP-complete for graphs with maximum degree four, for claw-free graphs, and even for (claw,diamond)-free graphs. In this talk we will consider induced subgraphs, among them are the *claw* ($K_{1,3}$), the *diamond* (the graph $K_4 - e$), the *butterfly* (two triangles sharing a vertex), and the generalized *net* $N_{i,j,k}$ (a triangle with three attached paths with i, j, k edges).

Our main result is a complete characterization of all 3-colourable (claw, diamond, H)-free graphs for $H \in \{N_{1,1,1}, N_{1,1,2}, N_{1,2,2}, N_{2,2,2}\}$. We will present a description of all non 3-colourable (claw, diamond, H)-free graphs for $H \in \{N_{1,1,1}, N_{1,1,2}, N_{1,2,2}, N_{2,2,2}\}$ in terms of butterflies. Moreover, we will show extensions of this characterization to larger graph classes.