

seminarium Matematyka Dyskretna

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3-colourability, diamonds and butterflies

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The 3-colourability problem is an NP-complete problem which remains NP-complete for graphs with maximum degree four, for claw-free graphs, and even for (claw,diamond)-free graphs. In this talk we will consider induced subgraphs, among them are the $claw(K_{1,3})$, the diamond (the graph K_4-e), the butterfly (two triangles sharing a vertex), and the generalized net $N_{i,j,k}$ (a triangle with three attached paths with i, j, k edges).

Our main result is a complete characterization of all 3-colourable (claw, diamond, H)-free graphs for $H \in \{N_{1,1,1}, N_{1,1,2}, N_{1,2,2}\}$. We will present a description of all non 3-colourable (claw, diamond, H)-free graphs for $H \in \{N_{1,1,1}, N_{1,1,2}, N_{1,2,2}\}$ in terms of butterflies. Moreover, we will show extensions of this characterization to larger graph classes.

- B. Randerath and I. Schiermeyer, Vertex colouring and forbidden subgraphs a survey, Graphs and Combinatorics 20 (2004) 1-40.
- [2] I. Schiermeyer and B. Randerath, Polynomial χ-Binding Functions and Forbidden Induced Subgraphs: A Survey, Graphs and Combinatorics 35 (1) (2019) 1–31.