



# SEMINARIUM MATEMATYKA DYSKRETNA

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## DENSE ON-LINE ARBITRARILY PARTITIONABLE GRAPHS

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A graph  $G$  of order  $n$  is called *arbitrarily partitionable* (AP for short) if, for every sequence  $(n_1, \dots, n_k)$  of positive integers with  $n_1 + \dots + n_k = n$ , there exists a partition  $(V_1, \dots, V_k)$  of the vertex set  $V(G)$  such that  $V_i$  induces a connected subgraph of order  $n_i$  for  $i = 1, \dots, k$ . In this paper we consider the on-line version of this concept. We prove that if  $G$  is a connected graph of order  $n \geq 15$  and size  $\|G\| > \binom{n-3}{2} + 6$ , then  $G$  is traceable unless  $G$  is a spanning subgraph of a unique exceptional graph. Further, if  $G$  is a connected graph such that  $\alpha(G) \leq \lceil \frac{n}{2} \rceil$  and the degrees sum of any pair of non-adjacent vertices is at least  $n - 3$ , then  $G$  is on-line arbitrarily partitionable except for two graphs of small orders. It follows that AP dense graphs are also on-line AP. This is in contrast to sparse graphs where only few AP graphs are on-line AP.

The talk will be given in English due to our foreign visitors.